#### Introduction – Chris Develder

- PhD, Ghent University, 2003
  - "Design and analysis of optical packet switching networks"



- Professor at Ghent University since Oct. 2007
  - Research Interests: dimensioning, modeling and optimizing optical (grid/cloud) networks; smart grids; multimedia and home networks; information retrieval
  - Visiting researcher at UC Davis, CA, USA, Jul-Oct. 2007 (optical grids)
  - Visiting researcher at Columbia Univ., NY, USA, 2013-14 (IR/IE)
- Industry Experience: network planning/design tools
  - OPNET Technologies (now part of Riverbed), 2004-05
- More info: <a href="http://users.atlantis.ugent.be/cdvelder">http://users.atlantis.ugent.be/cdvelder</a>











**ARCHITECTURE** 

# Dimensioning (optical) networks for cloud computing

Chris Develder, et al.

Ghent University – iMinds Dept. of Information Technology – IBCN

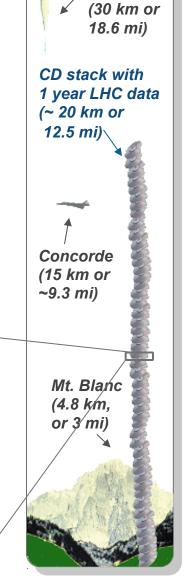




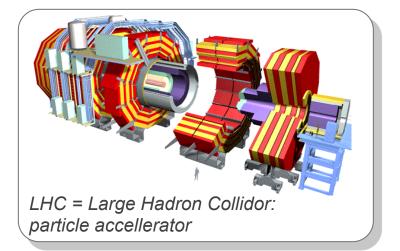
# **Background: "Optical grids"**

#### • eScience:

- By 2015 it is estimated that particle physicists will require exabytes (10<sup>18</sup>) of storage and <u>petaflops</u> (10<sup>15</sup>) per second of computation
- CERN's LHC Computing Grid (LGC), when fully operational generates <u>15 petabytes</u> annually (that's ~2Gbit/s)



Balloon









# "Optical grids" for consumer services?

#### E.g., video editing:

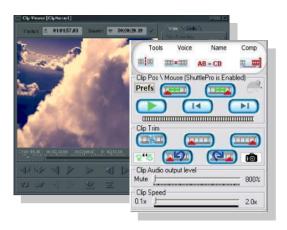
2Mpx/frame for HDTV, suppose effect requires 10 flops/px/frame, then evaluating 10 options for 10s clip is **50 Gflops** (today's high performance PC: <5 Gflops/s)



Online gaming: e.g. Final Fantasy XI: 1.500.000 gamers

<u>Virtual reality:</u> rendering of 3\*10<sup>8</sup> polygons/s → 10<sup>4</sup> GFlops





Multimedia editing

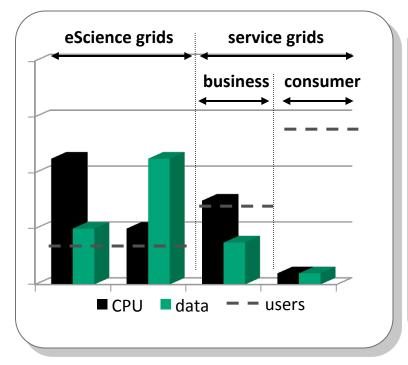


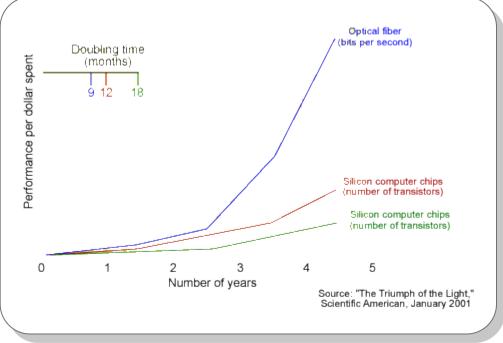


# Why optics? (3)

#### Conclusion:

- <u>Grid</u> opportunities ranging from academia over corporate business to home users
- Optical data speeds ≥ internal PC bus speeds
  - ⇒ network speed no bottleneck







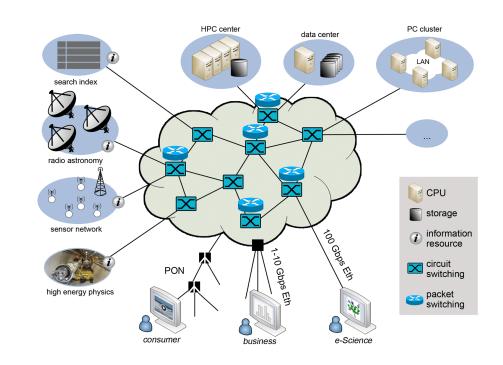




# Today: towards optical grid / cloud computing

Optical networks crucial for increasingly demanding cloud services, e.g.,

- Computing:
  - High energy physics
  - Amazon EC2, Microsoft Azure
- Online storage:
  - Dropbox, Google Drive, etc.
- Collaboration tools:
  - MSOffice 365, Google Doc
- Video streaming:
  - Netflix, YouTube

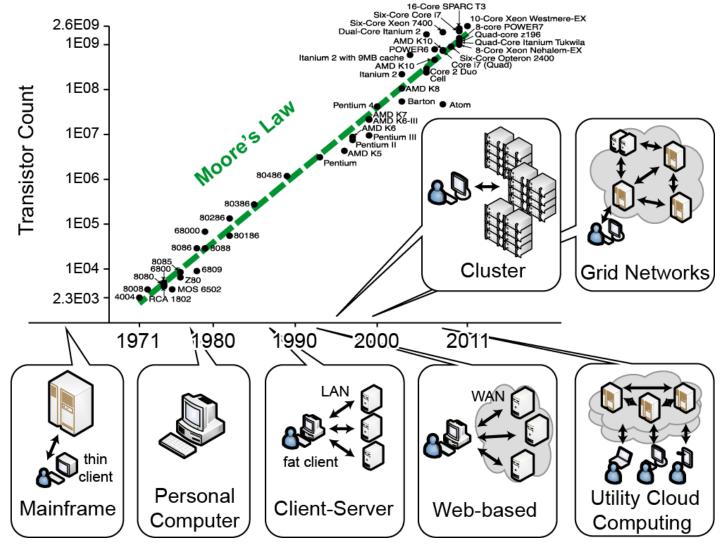


C. Develder, et al., "Optical networks for grid and cloud computing applications", Proc. IEEE, Vol. 100, No. 5, May 2012, pp. 1149-1167.





# A historical perspective ...







#### **Outline**

- 1. Introduction
- 2. Network dimensioning for clouds: What's different?
- 3. An iterative network + server dimensioning approach
- 4. Exploiting anycast for resilience purposes
- The next step: accounting for inter-DC synchronization
- 6. Wrap-up





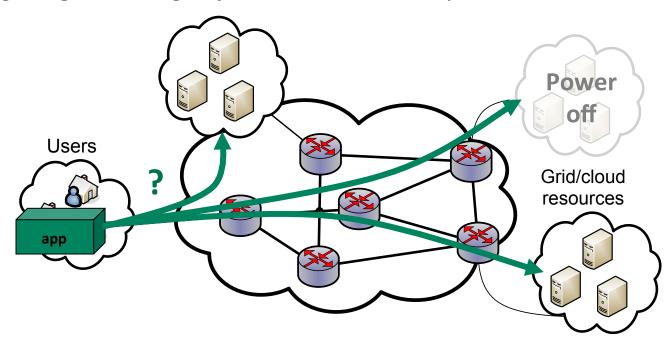
# Dimensioning for clouds: What's different?





# **Anycast**

- Users do (in general) <u>NOT</u> care where applications are served
  - E.g., virtual machines in laaS can be instantiated anywhere
  - E.g., bag-of-tasks grid jobs can be run at any server



J. Buysse, K. Georgakilas, A. Tzanakaki, M. De Leenheer, B. Dhoedt and C. Develder, "Energy-efficient resource provisioning algorithms for optical clouds", IEEE/OSA J. Opt. Commun. Netw., Vol. 5, No. 3, Mar 2013, pp. 226-239. doi:10.1364/JOCN.5.000226.





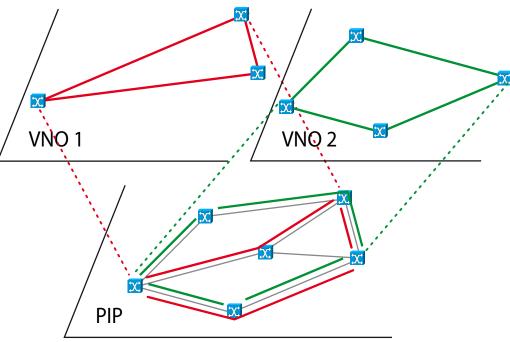


#### **Network virtualization**

Physical network is logically partitioned in isolated virtual networks

Virtual Network Operators
 (VNO) operate logically
 separated networks

Physical Infrastructure
 Providers (PIP) have full control over infrastructure (fibers, OXCs)



J.A. García-Espín, et al., "Logical Infrastructure Composition Layer: the GEYSERS holistic approach for infrastructure virtualisation", in Proc. TERENA Networking Conference (TNC 2012), Reykjavík, Iceland, 21-24 May 2012.





# An iterative network + server dimensioning approach and the impact of scheduling

C. Develder, B. Mukherjee, B. Dhoedt and P. Demeester, "On dimensioning optical Grids and the impact of scheduling", Photonic Netw. Commun., Vol. 17, No. 3, Jun. 2009, pp. 255-265. doi:10.1007/s11107-008-0160-z







#### **Problem Statement**

#### Given:

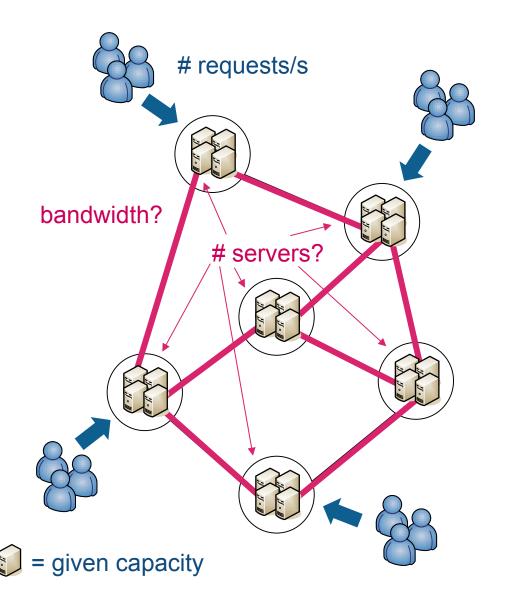
- Network topology
- Request arrival process
- Requested processing capacity
- Target maximum loss rate

#### Find

- Locations of servers,
- Amount of servers,
- Amount of link bandwidth

#### While

- Meeting max. loss
- Minimizing network capacity



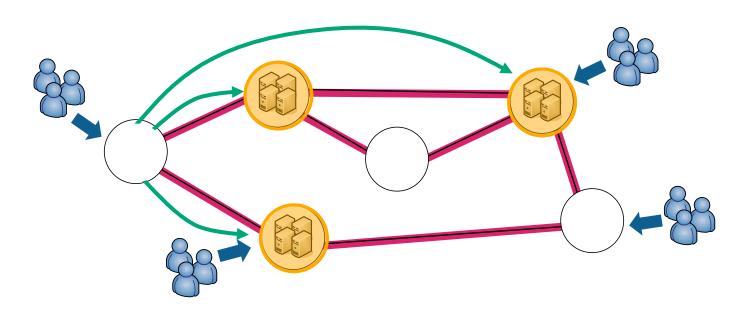






#### Solution

- Phased approach
  - 1 Determine K server locations (approx., ILP)
  - 2 Determine server capacity (analytical, ErlangB)
  - 3 Determine inter-site bandwidths (simulation)
  - 4 Dimension link bandwidths (= number of wavelengths)







# **Step 1:** Server locations

- Given:
  - Job arrivals at each site
  - Each source S site sends all its requests to a single destination D
     (simplifying assumption!)
  - Shortest path routing is used
- Find:
  - K server locations, minimizing total amount of used link bandwidth



≈ K-means clustering problem





# **Heuristic: k-means clustering**

#### • Algorithm\*:

- (1) Choose K points, representing initial group centroids
- (2) Form clusters: assign each object to closest centroid
- (3) Recalculate K centroids positions within their cluster
- (4) Repeat Steps 2-3 until the centroids no longer move

#### Our problem:

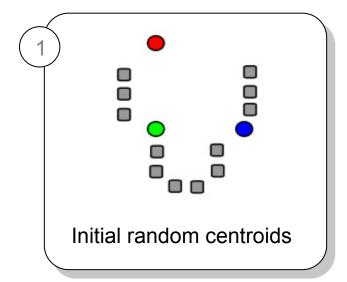
- k-medoid (i.e., centers are actual data points)
- "closest" = shortest path distance

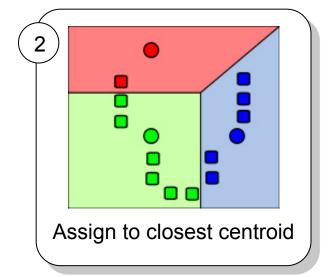
\*: J. B. MacQueen (1967): "Some Methods for classification and Analysis of Multivariate Observations", *Proc.* 5<sup>th</sup> Berkeley Symp. on Mathematical Statistics and Probability, Berkeley, University of California Press, 1:281-297

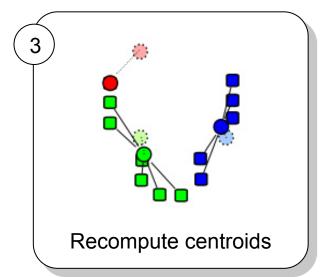


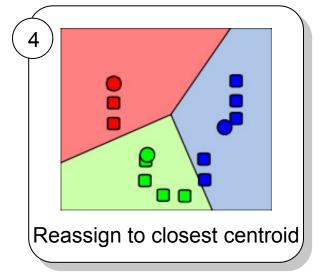


# **Heuristic: k-means clustering**







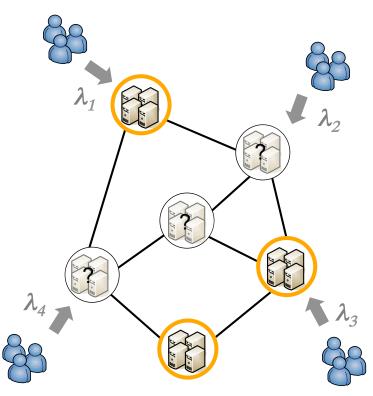






# Step 1: Finding the K "best" locations

- Binary variables:
  - $t_v = 1$  iff site v is server location
  - $f_{vv'}$  = 1 iff request from source v is directed to v'



#### Constants:

- $h_{vv'}$  = cost for sending 1 unit request from source v to server site v'
- $\Delta_v$  = number of unit requests from source v

$$\min \sum_{v} \sum_{v'} \Delta_{v} \cdot h_{vv'} \cdot f_{vv'}$$

subject to

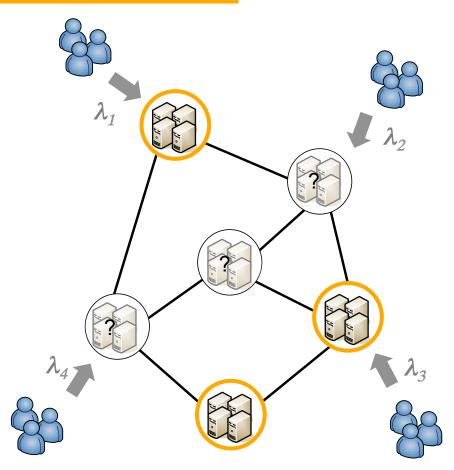
$$\begin{cases} \sum_{v} t_{v} = K \\ \sum_{v'} f_{vv'} = 1 \quad \forall v \\ f_{vv'} \le t_{v} \quad \forall v, v' \end{cases}$$





# **Step 1:** Server locations

Find K server locations:



$$\min \sum_{i} \sum_{j} \lambda_{i} \cdot H_{ij} \cdot S_{ij}$$

subject to

$$\begin{cases} \sum_{j} T_{j} = K \\ \sum_{j} S_{ij} = 1 \quad \forall i \\ S_{ij} \leq T_{j} \quad \forall i, j \end{cases}$$





# Step 1: ILP formulation

- Binary variables:
  - T<sub>i</sub> = 1 iff site j is chosen as cluster center (i.e., server location)
  - S<sub>ii</sub> = 1 iff site i belongs to cluster with center j (i.e., sends traffic to center j)
- Constants:
  - H<sub>ii</sub> = distance from site i to site j
  - $\lambda_i$  = job arrival rate at site i
- Objective:

$$\min \sum_{i} \sum_{j} \lambda_{i} \cdot H_{ij} \cdot S_{ij}$$

Constraints:

$$\sum_{j} T_{j} = K$$

$$\sum_{j} S_{ij} = 1 \quad \forall i$$

$$S_{ij} \leq T_j \quad \forall i, j$$

Only send traffic to centers





# Step 2: Server capacities

• Find number of servers *n*:

• 
$$L = ErlangB(n, \lambda, \mu) = \frac{(\lambda/\mu)^n/n!}{\sum_{k=0}^n (\lambda/\mu)^k/k!}$$

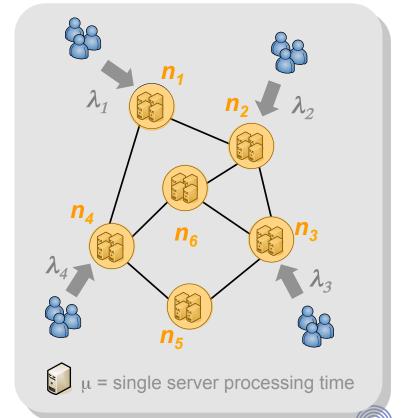
- Distribution among server sites: 3 alternatives
  - *unif*: uniformly distributed among all sites:  $n_i = n/N$
  - **prop**: proportional to local arrival rate:  $n_i = \lambda_i/(N \cdot \lambda)$
  - *lloss*: try to achieve the same (local) loss rate at each site:  $n_i \sim n'_i$  with  $L = ErlangB(n'_i, \lambda, \mu)$

L =target loss

 $\lambda$  = total arrival rate (all N sites)

 $\mu$  = single server processing time

n = total number of servers





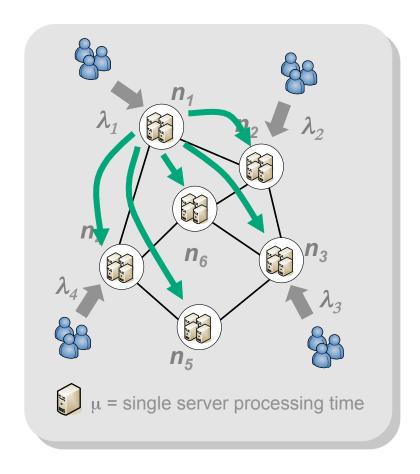
# Step 3: Inter-site bandwidth

#### Given:

- Request arrivals
- Site server capacities

#### Find

- Bandwidth exchanged between sites (i.e., amount of requests)
- Scheduling alternatives: <u>alwayst try</u> <u>local</u>, if busy then
  - SP: shortest path (i.e., closest free server)
  - rand: randomly pick a free site
  - mostfree: choose site with most free servers







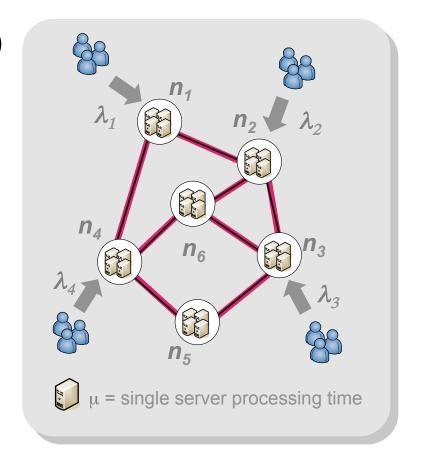
# **Step 4:** Link dimensions

#### Given:

- Inter-site request arrivals (from step 2)
- Shortest path routing (assumption)

#### Find

• Link bandwidth (amount of wavelengths)

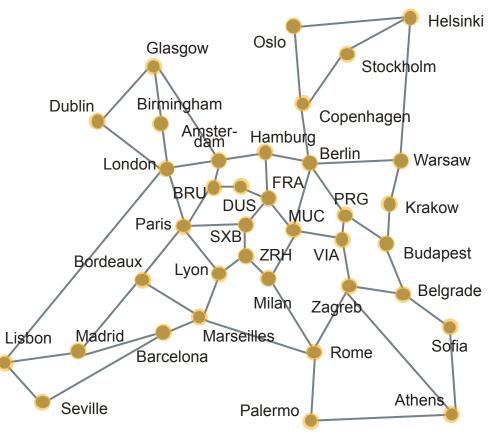






# **Case study**

- Topology:
  - EU topology
  - 37 nodes
  - 57 links
- Request arrivals  $\lambda_i$ :
  - Random
  - 30% uniformly in [1,15], 70% uniformly in [30,60]
- Server capacity:
  - 1 request / time unit
- ErlangB:
  - Max. 5% loss
    - ⇒ 799 servers

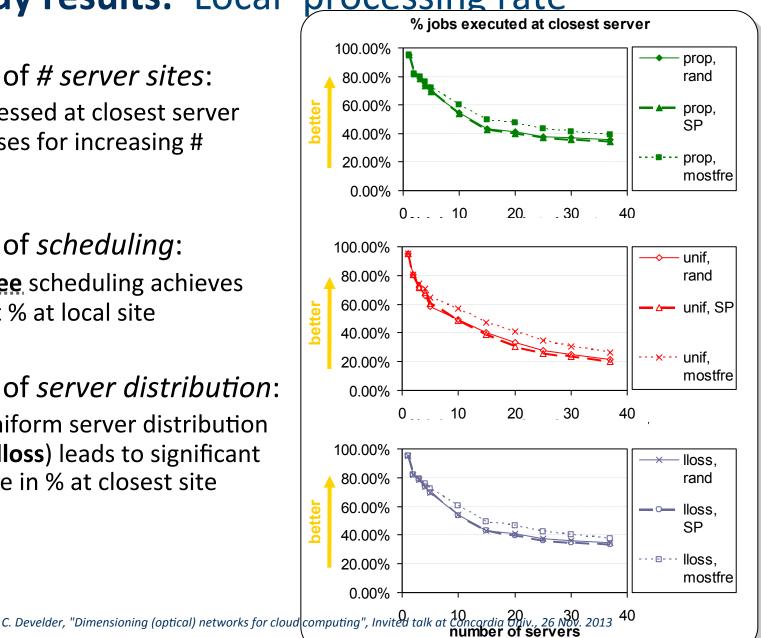






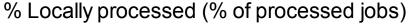
Case study results: 'Local' processing rate

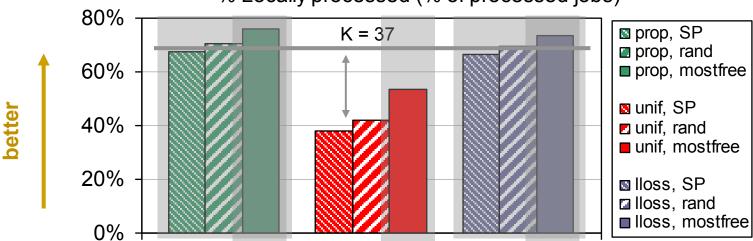
- Influence of # server sites:
  - % processed at closest server decreases for increasing # servers
- Influence of scheduling:
  - mostfree scheduling achieves highest % at local site
- Influence of server distribution:
  - Non-uniform server distribution (**prop**, **lloss**) leads to significant increase in % at closest site





# Case study results: 'Local' processing rate





- Server distribution:
  - unif: uniformly distributed
  - prop: ~ local arrival rate
  - Iloss: ~ same (local) loss rate

- Scheduling: local first, if busy then...
  - SP: shortest path
  - rand: randomly pick a free site
  - **mostfree**: site with most free servers

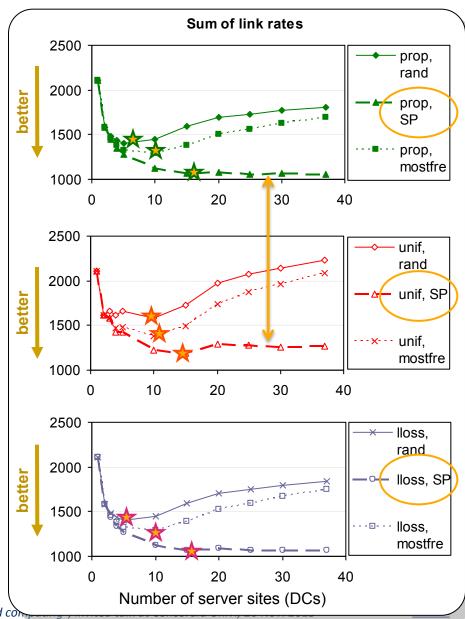
- Conclusions:
  - mostfree achieves highest local processing
  - Intelligent server placement (prop, lloss) achieves higher local processing





# Case study results: Link bandwidths

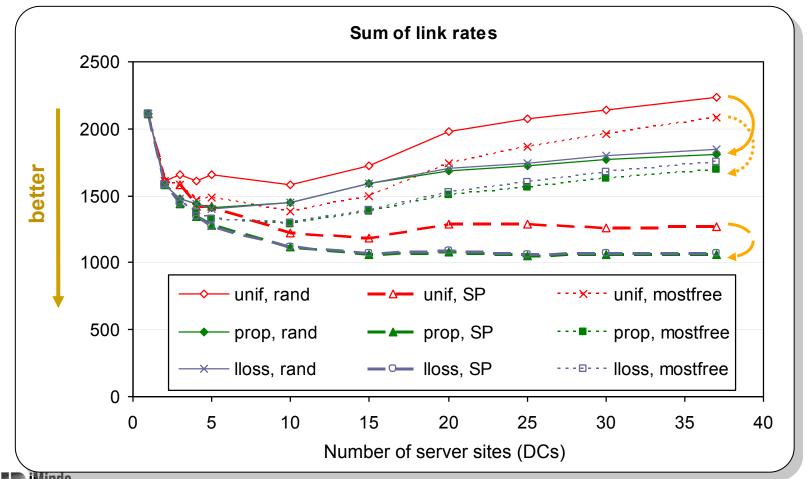
- Influence of # server sites:
  - There is an "optimal" value, depending on the scheduling algorithm & server distribution
- Influence of scheduling:
  - SP scheduling obviously leads to lowest total link bandwidth
- Influence of *server distribution*:
  - Non-uniform server distribution (prop, lloss) leads to significant BW reduction





# Case study results: Link bandwidths

- Influence of server distribution:
  - Non-uniform distribution leads to significant BW reduction





# **Conclusions wrt dimensioning**

- Proposal of dimensioning approach
  - Sequential approach (first server locations & dimensions, then network)
  - Combination of analytics and simulation
- Comparison of site dimensioning and scheduling alternatives
  - Dimensioning: intelligent server placement allows higher local processing
  - Scheduling: maximizing "local" processing may come at link bandwidth price





# **Exploiting anycast for <u>resilience</u>**

C. Develder, J. Buysse, B. Dhoedt and B. Jaumard, "Joint dimensioning of server and network infrastructure for resilient optical grids/clouds", IEEE/ACM Trans. Netw., Vol. PP, Oct. 2013, pp. 1-16. doi:10.1109/TNET.2013.2283924







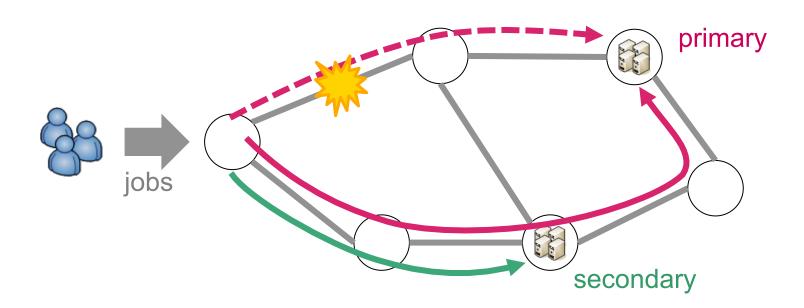
#### **Exploiting relocation for resilience?**

#### Goal:

Achieve (network) dimensioning, for resiliency against failures

#### Idea:

Exploit anycast principle: allow rerouting jobs to other destination

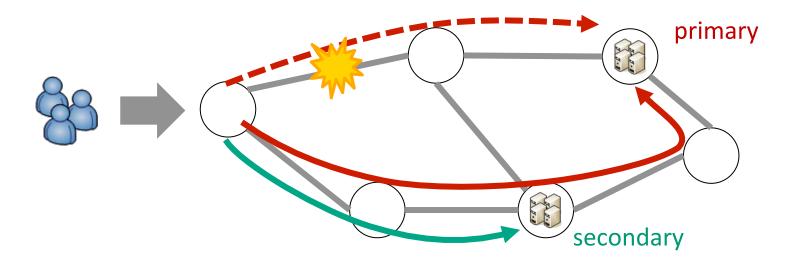






# **Exploiting relocation**

- Dimension optical grid/cloud so that it is resilient against failures
- Exploit anycast principle: allow rerouting to other destinations



J. Buysse, M. De Leenheer, B. Dhoedt and C. Develder, "Providing resiliency for optical grids by exploiting relocation: A dimensioning study based on ILP", Comput. Commun., Vol. 34, No. 12, Aug. 2011.

A. Shaikh, J. Buysse, B. Jaumard and C. Develder, "Anycast routing for survivable optical grids: scalable solution methods and the impact of relocation", IEEE/OSA J. Opt. Commun. Netw., Vol. 3, No. 9, Sep. 2011.







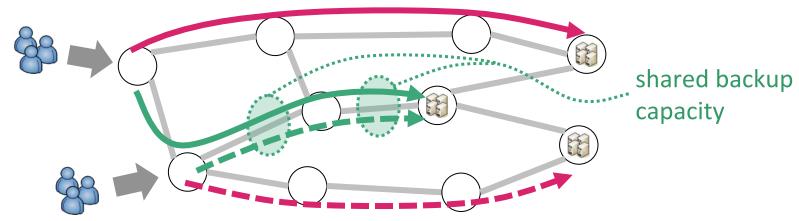
#### **Problem statement**

#### Given:

- Topology w/ K chosen server locations (i.e., data centers)
- Traffic "vector": sources + volume of traffic

#### • Find:

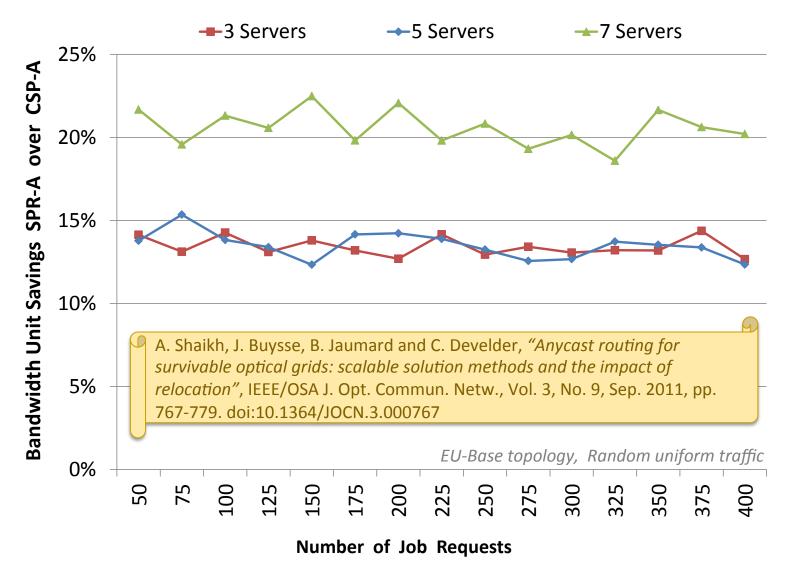
- Primary and secondary <u>routes</u> for each demand, while
- Minimizing resource dimensions (in terms of # wavelengths/link, # servers)
- For the case of <u>shared protection</u> (+ relocation) against single failures







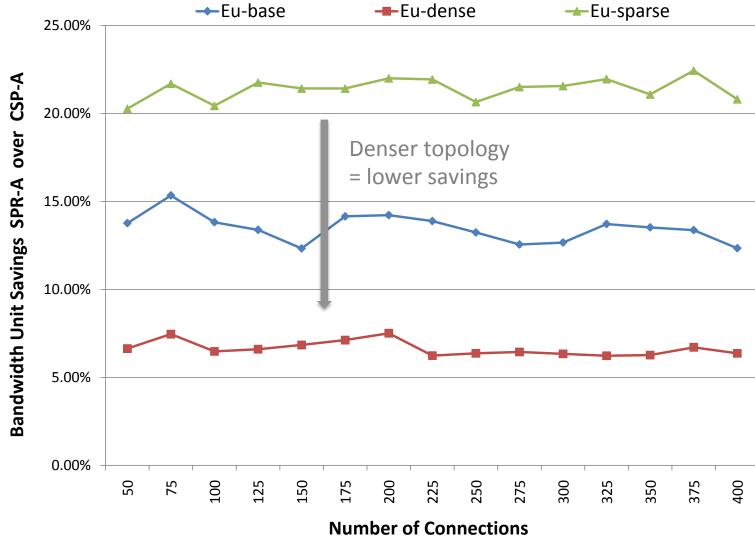
# Initial results on network savings







# Initial results on network savings







#### **Problem statement**

#### Given

- Topology (sources, <u>candidate</u> data center locations, OXCs)
- Demand (for given sources)
- <u>Survivability</u> requirements (e.g., link and/or node failures)

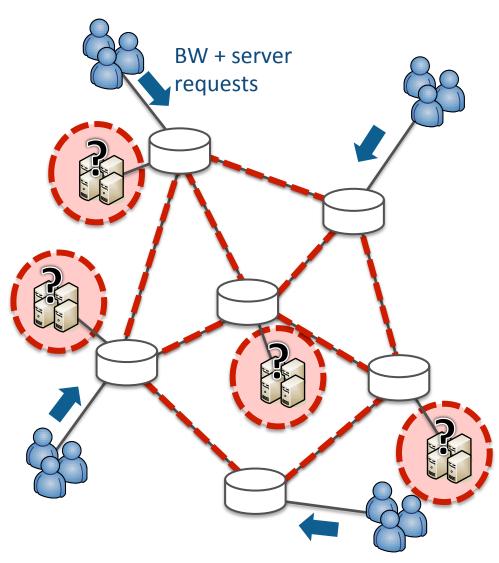
#### **Find**

Shared protection

- K locations (chosen from candidate data center locations)
- Destination sites and routes
- Network and server capacity

#### Such that

 Network and server resources are minimized







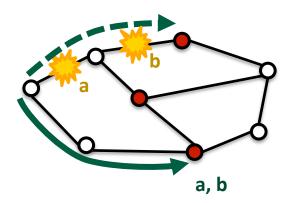


## Solution approach

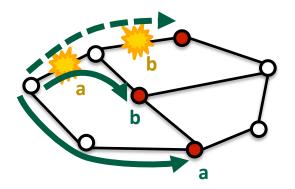
**Step 1: Find the K best data center locations** 

Step 2: Find the primary/secondary destinations + paths towards them

Failure-Independent (FID)
rerouting
=> Column generation



Failure-Dependent (FD)
rerouting
=> Single ILP

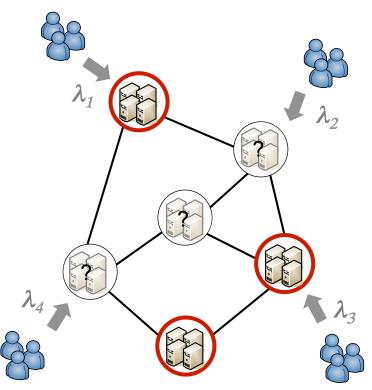






# Step 1: Finding the K "best" locations

- Binary variables:
  - $t_v = 1$  iff site v is server location
  - $f_{vv'v''}$  = 1 iff request from source v is directed to primary v', backup v''



#### Constants:

- $h_{vv'v''}$  = cost for sending 1 unit request from source v to server sites v', v''
- $\Delta_v$  = number of unit requests from source v

$$\min \sum_{v} \sum_{v'} \Delta_{v} \cdot h_{vv'} \cdot f_{vv'v''}$$

subject to

$$\begin{cases} \sum_{v} t_{v} = K \\ \sum_{v'} \sum_{v''} f_{vv'v''} = 1 \quad \forall v \\ f_{vv'v''} \leq t_{v'} \quad \forall v, v', v'' \\ f_{vv'v''} \leq t_{v'} \quad \forall v, v', v'' \end{cases}$$





Network model: **Network capacity** (wavelengths) WDM network Grid/cloud users Data center (traffic source) (traffic destination) Data center capacity (servers)

- $w_l$  = "capacity" of link l
- Capacity = wavelengths for NET links, servers for DST links!

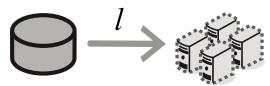




- Failure: modeled as SRLG = set of links s that simultaneously fail
- Single link failure:

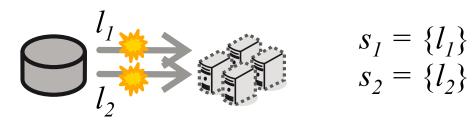
$$S = \{l, l'\}$$

- Single server failure: 1:N protection [= add 1 for each case single one out of N fails]
  - No relocation:
    - Let x = number of servers under working conditions



$$w_l \ge \rho_l \cdot x$$
$$\rho_l = 1 + 1/N$$

- Then we need  $\left[ (1+1/N) \cdot x \right]$  servers
- Relocation: consider (1+N) parallel links, at most 1 fails







- Failure dependent (FD) rerouting => Single ILP
- Variables:
  - $p_{vls}$ : number of unit demands with source v that cross link l under failure s
  - $w_l$ : capacity on link l

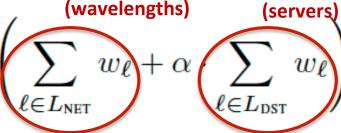
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Network capacity

**Data center capacity** 

Objective:

min



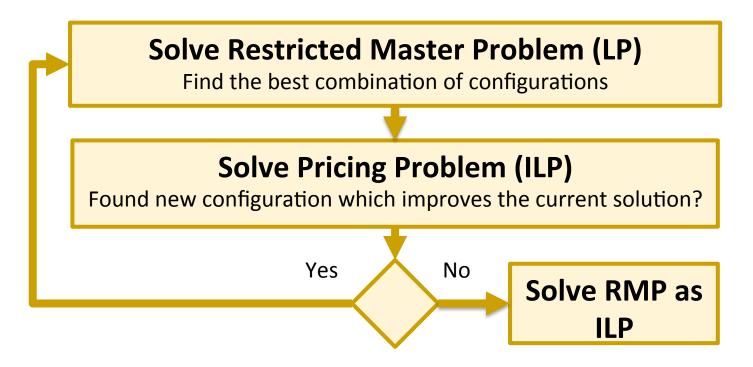
- Constraints:
  - $p_{vls}$ : flow constraints + don't use failing links when protecting against s
  - $w_l$ : count capacity 1 for network link 1+1/N for server link, in case of relocation

$$w_{\ell} \ge \underbrace{\rho_{\ell}} \sum_{v \in V_{\text{SPC}}} p_{v\ell s} \qquad \forall s \in S$$





- Failure-independent (FID) rerouting => Column generation:
  - Assume: given "configurations" = combination of working and backup paths
  - Restricted Master Problem (RMP) finds best combination of configurations
  - Pricing Problem (PP) finds new configuration that can reduce cost







## Finding initial configurations for RMP of Step 2

- Configuration associated with a particular source
  - Working path to primary destination
  - Backup path to secondary destination
- Algorithm:

Suurballe's algorithm

- Find shortest 2 disjoint paths from s to candidate destination(s):
   configuration c
- Create new configurations that share backup links:

Sharing of backup wavelengths

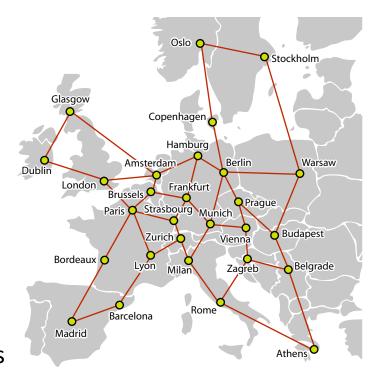
- Remove working links of c
- For all configurations c' with primary disjoint from c:
   set backup link weights to 0
- Find backup path b" as shortest path to candidate destination in reduced graph
- Create c": primary of c, and b" as secondary





## Case study set-up

- Topology
  - European network
  - 28 nodes and 41 bidirectional links
- Demand
  - Randomly generated requests (10-350)
  - 10 instances for each number of requests



#### Four scenarios:

No relocation Exploiting relocation

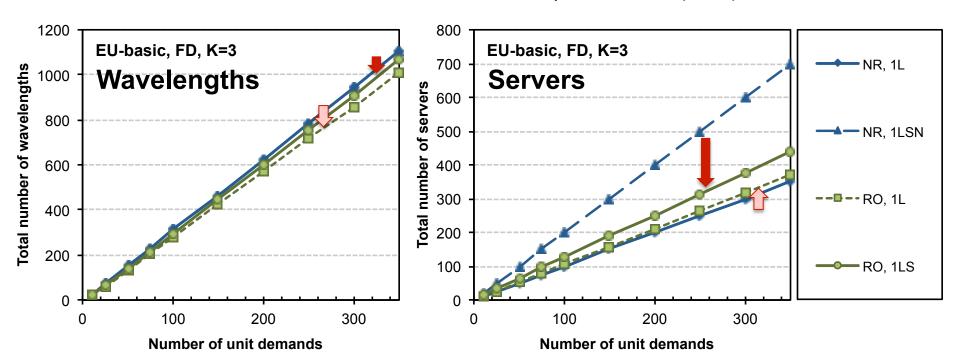
Single <u>link</u> failures: **1L, NoReloc 1L, Reloc** 





### The impact of relocation

- Single Link failures (1L):
  - Reduction of backup wavelengths
  - Slight increase in server capacity
- Single link/server failure (1LS)
  - Reduction of backup wavelengths
  - Fewer servers than 1:N server protection (N=1)

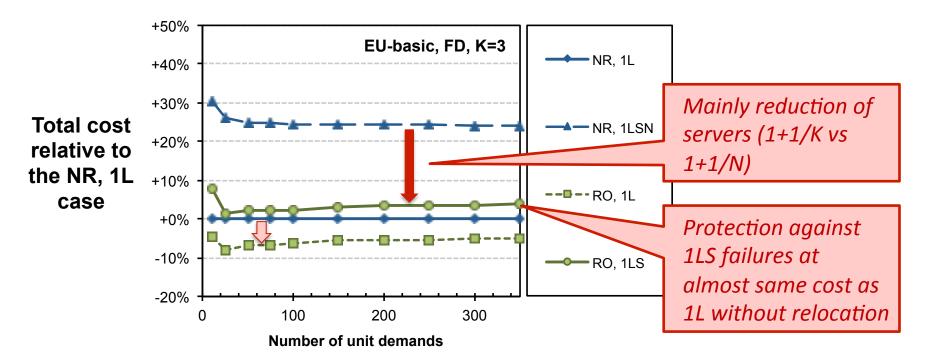






#### The impact of relocation

- Single Link failures (1L):
  - Reduction of backup wavelengths
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- Single link/server failure (1LS)
  - Reduction of backup wavelengths
  - Fewer servers than 1:N server protection (N=1)

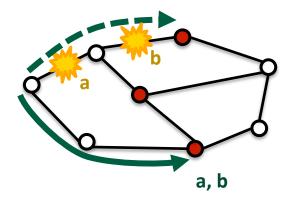




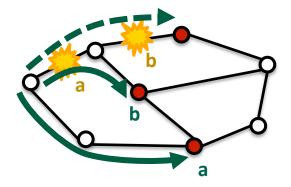


## Failure dependent rerouting? (FD vs FID)

Failure-Independent (FID) rerouting



Failure-Dependent (FD) rerouting

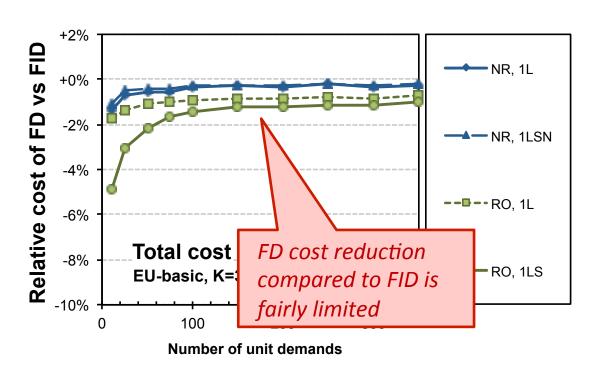


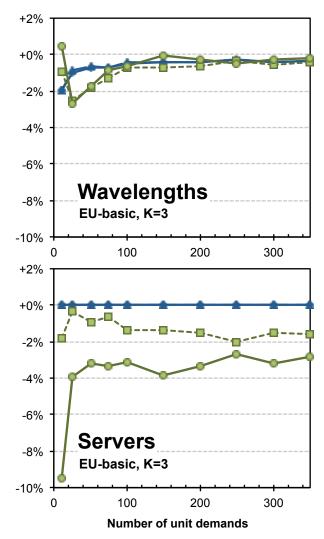




## Failure dependent rerouting? (FD vs FID)

- FD is best, obviously
- Yet, difference is limited (few %)
  - at least for small K (= number of server sites)









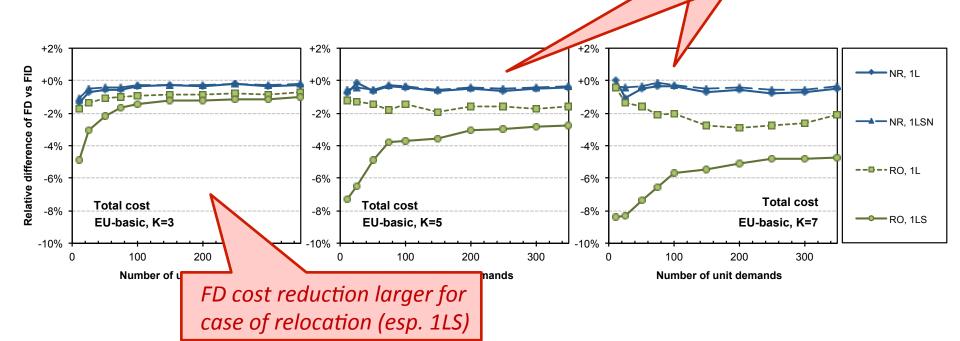
## Failure dependent rerouting? (FD vs FID)

FD is best, obviously

Yet, difference is limited (few %)

— at least for small K (= number of server sites)

FD advantage increases for larger number of server sites!



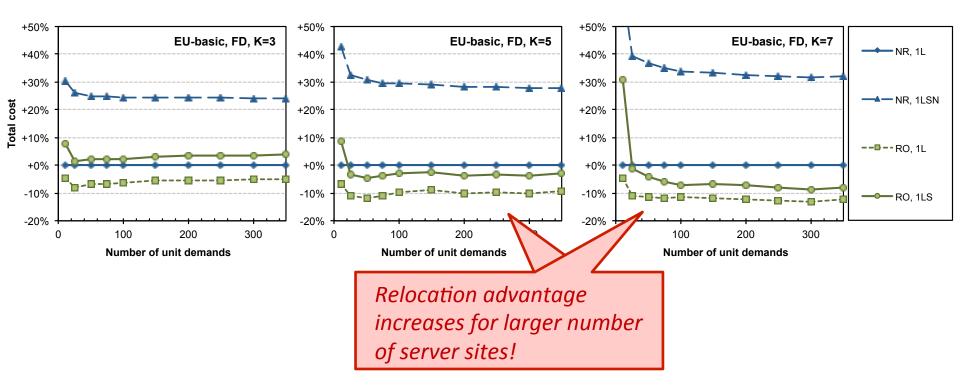




#### Influence of K on benefit of relocation?

#### • K **7**

- Wavelength reduction more pronounced
- Lower extra cost to provide single server failure protection







#### **Conclusions**

- Dimensioning algorithm for resilient optical grids
  - Exploit relocation for resiliency
  - Compact ILP for finding K best locations
  - ILP (w/ column generation) for server & network dimensions
  - Generic model based on SRLG concept
- Case study on EU network topology [10-350 unit demands]
  - Relocation offers cost advantage of up to ca. 10% to protect against single network link failures
  - Total cost to protect against 1LS with relocation
     ≈ Cost to protect against 1L only, without relocation
  - Relocation advantage more substantial for larger number of server sites
  - Failure-dependent rerouting advantage if we use relocation (couple of %)





# The next step: virtualization & accounting for server synchronization

M. Bui, B. Jaumard and C. Develder, "Anycast end-to-end resilience for cloud services over virtual optical networks (Invited)", in Proc. 15th Int. Conf. Transparent Optical Netw. (ICTON 2013), Cartagena, Spain, 23-27 Jun. 2013. doi:10.1109/ICTON.2013.6603032







#### Resiliently provisioning virtual cloud networks

#### How to choose the virtual to physical mapping, such that

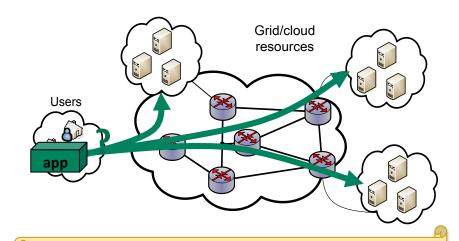
Services remain available in case of network failures



Bandwidth for providing services is minimal

#### Note:

- Anycast: requests coming from users can be served by any server
- Cloud services offered by VNO
- Cloud services run on top PIP



B. Jaumard, A. Shaikh and C. Develder, "Selecting the best locations for data centers in resilient optical grid/cloud dimensioning (Invited Paper)", in Proc. 14th Int. Conf. Transparent Optical Netw. (ICTON 2012), Coventry, UK, 2-5 Jul. 2012.

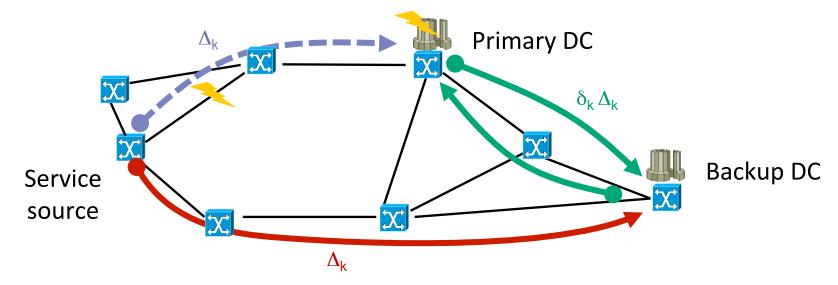




#### **Protection scheme concept**

- Covered failures
  - Network links -> disjoint primary and backup paths
  - Data centers 

    disjoint primary and backup server locations



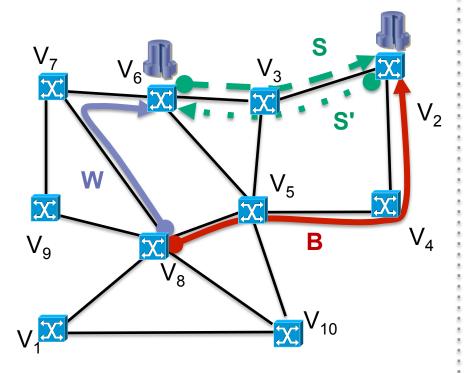
- Note: synchronization between data centers for smooth failover switching!
  - We assume: sync needs fraction  $\delta$  of service bandwidth  $\Delta$



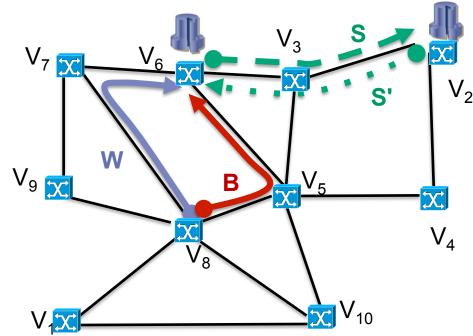


#### Two proposed protection schemes

Scheme 1: VNO-resilience



Scheme 2: PIP-resilience







#### **Related work**

- Traditional dimensioning (no virtualisation, no resilience):
  - Develoer et al. 2009: Anycast, flexibility in choosing data center
- Resilient dimensioning problem:
  - Shaikh et al. 2011, Develder et al. 2012: scalable method, no synchronization between working and backup DCs
- Routing cloud service requests and mapping a VNet to the physical infrastructure separately:
  - Lee et al. 2009, Yu et al. 2010: Survivable VNet embedding, but assume VNet is given
  - Jiang et al. 2012, Alicherry et al. 2012: Optimal server selection and routing of anycast services in the physical layer for intra- and inter-DC networks but no resilient network design in the virtual layer
- VNet planning problem:
  - Barla et al. 2012, Barla et al. 2013: using mixed integer linear programming, but no synchronization between working and backup DCs





#### **Problem statement**

#### Given

- Cloud network topology: G = (V, L), with V = nodes, L = links
- Locations of the data centers,  $V_D \subseteq V$
- Set of service requests, K
  - $v_k$ : source of service
  - $\Delta_k$ : bandwidth requirement
  - Services originating from the same source are aggregated

#### **Find**

- Choice of primary and backup DC locations for each service
- Primary, backup <u>and synchronization</u> paths

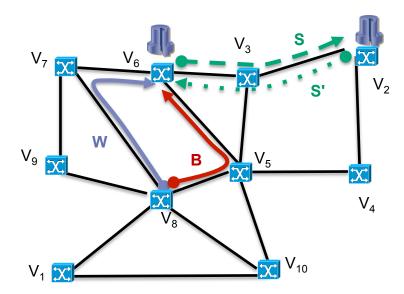
Such that total used network bandwidth utilization is minimized





#### Solution: Column generation model

- Column generation idea:
  - Many different "configurations"
  - Start from a restricted subset of such "configurations"
  - Iteratively find additional configurations that reduce the cost:
    - (1) Restricted Master Problem (RMP)
    - (2) Pricing Problem (PP) to find new configs
- A configuration =
  - Working path
  - Backup path
  - 2 sync paths, one in each direction, between the primary & backup DCs
  - Set of services protected by the set of 4 paths

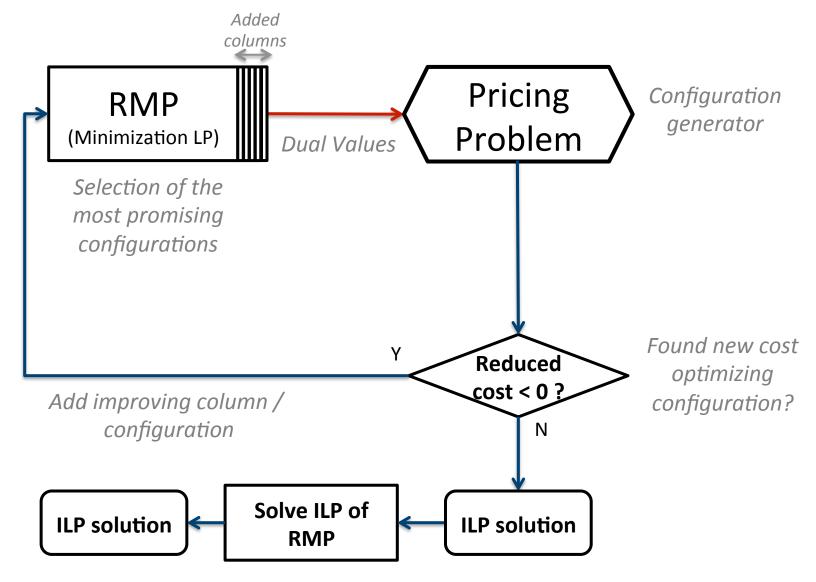








#### Column generation solution algorithm







### **Master problem**

- F set of failure sets. Each  $\mathcal{F} \subseteq F$  contains links that fail at the same time.
- *C* set of configurations *c*, associated with a source node *v*:
  - $p^w$ : working path from v to primary datacenter DC<sup>W</sup>
    - $p_{\ell}^{W}$  = 1 if link  $\ell$  used by the working path
  - $p^B$ : backup path from v to primary datacenter DC<sup>W</sup> (model 1) or backup datacenter DC<sup>B</sup> (model 2)
    - $p_{\ell}^{\rm B}$  = 1 if link  $\ell$  is used by the backup path
  - p<sup>s</sup>: synchronization path from DC<sup>W</sup> to DC<sup>B</sup>
  - ps': synchronization path from DC<sup>B</sup> to DC<sup>W</sup>
- $\alpha_k$  = 1 if service k is routed and protected by configuration c
- $b_\ell^{ ext{W}}$  working synchronization bandwidth requirement on  $\ell \in p^s$
- $b_\ell^{
  m S}$  primary-to-backup synchronization bandwidth requirement on  $\ell \in p^{s'}$
- ullet  $eta_\ell^{
  m W}$ is the working bandwidth and  $eta_\ell^{
  m B}$  is the backup bandwidth on link  $\ell$





## **Restricted Master Problem (RMP)**

Objective:

$$\min \quad \sum_{\ell \in L} \; (eta_\ell^{ ext{W}} \; + \; eta_\ell^{ ext{B}})$$

working backup

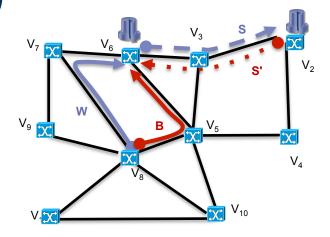
Constraints:

$$\begin{split} \beta_{\ell}^{\mathrm{W}} + \beta_{\ell}^{\mathrm{B}} &\leq W_{\ell} \\ \beta_{\ell}^{\mathrm{W}} &= \sum_{c \in C} \left( b_{\ell}^{\mathrm{W},c} + b_{\ell}^{\mathrm{S},c} \right) z_{c} \\ \sum_{c \in C} \alpha_{k}^{c} z_{c} &\geq 1 \\ \sum_{v \in V} \sum_{c \in C_{v}} \left( b_{\ell}^{\mathrm{W},c} \, p_{\ell'}^{\mathrm{B},c} + \sum_{k \in K_{v}} \Delta_{k} \, \alpha_{k}^{c} \, p_{\ell}^{\mathrm{W},c} \delta_{k} p_{\ell'}^{\mathrm{S}',c} \right) \, z_{c} \, \leq \beta_{\ell'}^{\mathrm{B}} \end{split}$$



 $z_c \in \{0, 1\}$ 

 $\beta_{\ell}^{W} \in \mathbb{R}$ 



$$\ell \in L$$

$$\ell \in L$$
 (3)

$$k \in K$$
 (4)

$$\ell \in F, F \in \mathcal{F}, \ell' \in L \setminus F$$
 (5)

$$c \in C$$
 (6)

$$\ell \in L \tag{7}$$

(2)

## **Pricing Problem (PP)**

#### Minimize

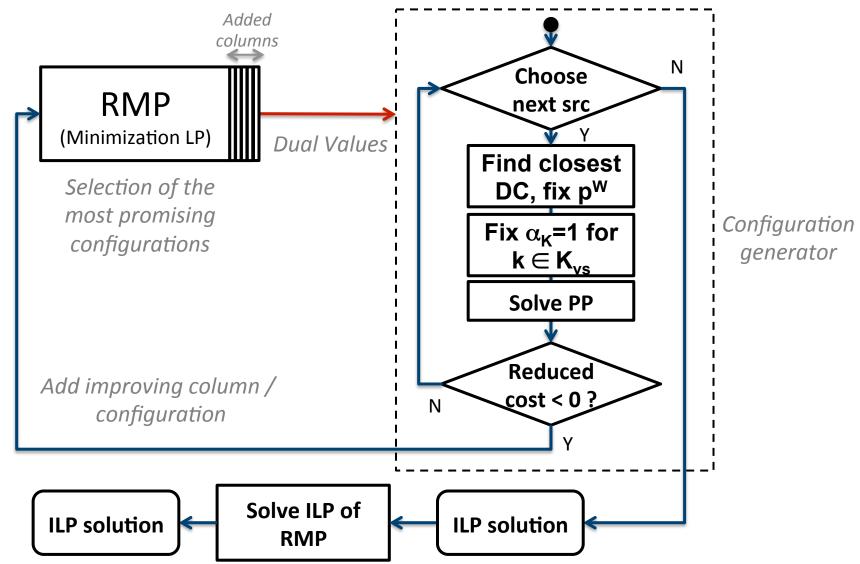
$$\begin{aligned} \overline{\text{COST}} &= \sum_{\ell \in L} u_{\ell}^{(3)} \left( b_{\ell}^{\text{W}} + b_{\ell}^{\text{S}} \right) - \sum_{k \in K} u_{k}^{(4)} \; \alpha_{k} - \sum_{F \in \mathcal{F}} \sum_{\ell \in F} \sum_{\ell' \in L: \ell \neq \ell'} \sum_{k \in K_{v_{\text{S}}}} u_{\ell \ell' F}^{(5)} \; \Delta_{k} \; \alpha_{k} \; p_{\ell}^{\text{W}} \left( p_{\ell'}^{\text{B}} + \delta_{k} \; p_{\ell'}^{\text{S}'} \right) \\ &= \sum_{\ell \in L} u_{\ell}^{(3)} \left( b_{\ell}^{\text{W}} + b_{\ell}^{\text{S}} \right) - \sum_{k \in K} u_{k}^{(4)} \; \alpha_{k} \; - \sum_{F \in \mathcal{F}} \sum_{\ell \in F} \sum_{\ell' \in L: \ell \neq \ell'} u_{\ell \ell' F}^{(5)} \; b_{\ell}^{\text{W}} \; p_{\ell'}^{\text{B}} \\ &- \sum_{F \in \mathcal{F}} \sum_{\ell \in F} \sum_{\ell' \in L: \ell \neq \ell'} \sum_{k \in K_{v_{\text{S}}}} u_{\ell \ell' F}^{(5)} \; \Delta_{k} \; \delta_{k} \; \alpha_{k} \; p_{\ell}^{\text{W}} \; p_{\ell'}^{\text{S}'} \end{aligned}$$

Cubic and square terms!





### Column generation solution algorithm - Heuristic

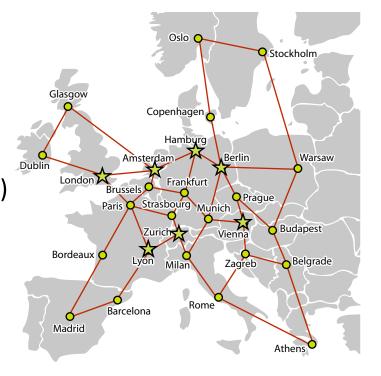






## **Case study**

- Topology:
  - European network
  - 28 nodes and 41 bidir links (= 82 directed)
- Two choices of 4 data centers (DCs)
  - Scattered evenly:
     Lyon, Berlin, London, Vienna
  - Pairs of close data centers:
     Amsterdam, Hamburg, Lyon, Zurich



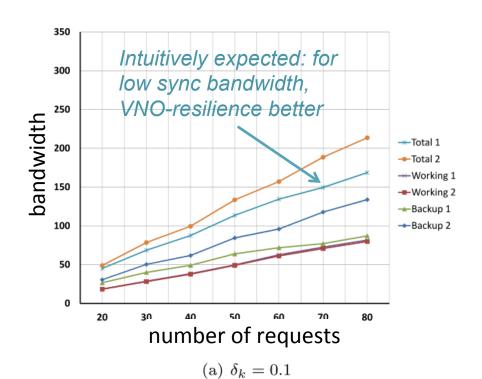
- Synchronization bandwidth fraction:  $\delta_k$  = 0.1 or 0.9
- Requests generated randomly with bandwidth in [0,1] wavelengths

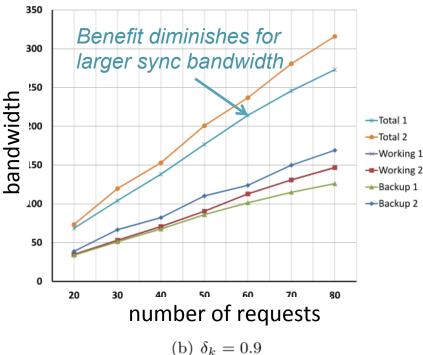




#### Results: evenly distributed DCs

- DCs in Lyon, Berlin, London, and Vienna
- Model 1: VNO-resilience, Model 2: PIP-resilience



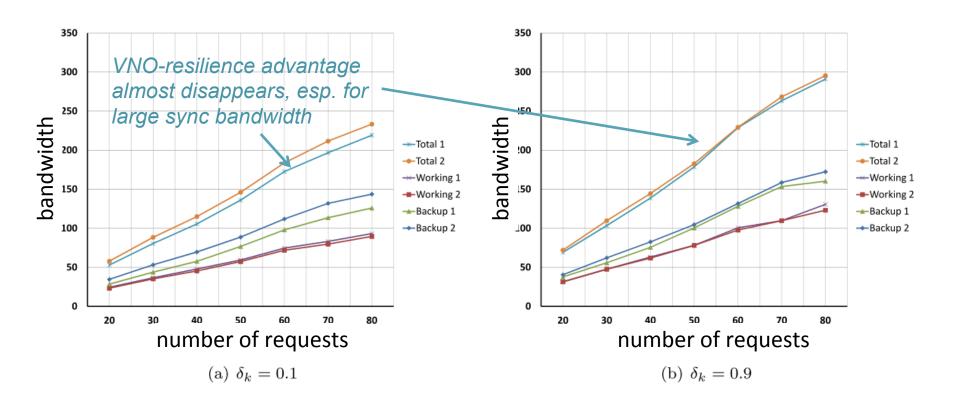






### Results: *close DC pairs*

- DCs in Amsterdam, Hamburg, Lyon, Zurich
- Model 1: VNO-resilience, Model 2: PIP-resilience







#### **Conclusions**

- Scalable column-generation based method for resilient VNet planning
- Intuition: VNO-resilience has lower physical network requirements than PIP-resilience
- But... relative advantage of VNO-resilience may be limited
  - When accounting for synchronization bandwidth between DCs
  - If DCs occur in nearby locations
- Future work:
  - Optimization of choice of DC locations?
  - Incorporate DC capacity constraints (e.g., limit max load)





# Wrap-up





#### **Take-away points**

- Characteristics of cloud computing:
  - Anycast: User does not greatly care of exact location of servers
  - Virtualization: Cloud service provider may want isolation
- Dimensioning cloud networks:
  - Network + DC: locations of data centers can be optimized
  - Shared protection: exploit anycast through relocation
  - Failure-dependent (FD) vs -independent (FID) routing: limited advantage of FD for small number of data center locations
  - Virtualization: VNO vs PIP resilience: VNO savings can be limited for certain data center location strategies





## Thank you ... any questions?



